Comparison of two different approaches for the analysis of data from a prospective cohort study: an application to work related risk factors for low back pain

W E Hoogendoorn, P M Bongers, H C W de Vet, J W R Twisk, W van Mechelen, L M Bouter

Aims: To compare the results of a traditional approach using standard regression for the analysis of data from a prospective cohort study with the results of generalised estimating equations (GEE) analysis.

Methods: The research was part of a three year prospective cohort study on work related risk factors for low back pain. The study population consisted of a cohort of 1192 workers with no low back pain at baseline. Information on work related physical and psychosocial factors and the occurrence of low back pain was obtained by means of questionnaires at baseline and at the three annual follow up measurements. In a traditional standard logistic regression model, physical and psychosocial risk factors at baseline were related to the cumulative incidence of low back pain during the three year follow up period. In a GEE logistic model, repeated measurements of the physical and psychosocial risk factors were related to low back pain reported at one measurement point later.

Results: The traditional standard regression model showed a significant effect of flexion and/or rotation of the upper part of the body (OR = 1.8; 95% CI: 1.2 to 3.0), but not of moving heavy loads (OR = 1.4; 95% CI: 0.7 to 3.1). The GEE model showed a significant effect of both flexion and/or rotation of the upper part of the body (OR = 2.2; 95% CI: 1.5 to 3.3) and moving heavy loads (OR = 1.5; 95% CI: 1.0 to 2.4). No significant associations with low back pain were found for the psychosocial work characteristics with either method, but the GEE model showed weaker odds ratios for these variables than the traditional standard regression model.

Conclusions: Results show that there are differences between the two analytical approaches in both the magnitude and the precision of the observed odds ratios.

In occupational health research on work related risk factors for musculoskeletal symptoms, there is an increasing awareness that prospective cohort studies are necessary to obtain more insight into the temporal relation between work related risk factors and health outcomes. Traditionally, these studies have mainly focused on examination of the relation between exposure measured at baseline and occurrence of the health outcome of interest during a specified follow up period. However, changes at the workplace may invalidate baseline data, and repeated measurements of exposure should therefore be considered. A recent review of studies on physical risk factors for back pain showed that hardly any cohort studies incorporated repeated measurements of exposure, although there were many studies with an extremely long follow up period during which the exposure could have changed considerably.

Repeated measurements can be made of both exposures and outcomes. The generalised estimating equation (GEE) method developed by Liang and Zeger is one of the methods that can be used for the analysis of repeated measurements. The GEE method extends standard regression analysis, taking into account the correlation between repeated measurements. The marginal distribution of the outcome is modelled, which means that GEE models describe the average occurrence of the outcome for the group as a whole over time. Data on a person at a certain time during follow up are included, whether or not data on that person are missing at other times, under the assumption that the pattern of missing data is random. The GEE method can be applied to a wide range of familiar models, including linear and logistic regression, which means that the method is suitable for the analysis of both continuous and dichotomous outcome variables. In addition, both time dependent and time independent covariates can be included.

Gender is a typical example of a time independent variable. All variables that are subject to change are, in principle, time dependent.

The Study on Musculoskeletal disorders, Absenteeism, Stress, and Health (SMASH) was a three year prospective cohort study among a working population, which was initiated to identify risk factors for musculoskeletal disorders. In this study, repeated measurements were made of both exposures and outcomes. In previous reports on the study, a traditional approach was used for the data analysis, implying that work related risk factors at baseline were related to the cumulative incidence of low back pain reported during follow up in a standard regression. The objective of the study described in this paper was to compare the results of this traditional approach with the results of a GEE analysis that includes the repeated measurements of exposure and outcome, to find out whether the latter approach produces different parameter and standard error estimates. For this purpose, both analytical approaches were applied to examine the relation between selected work related physical and psychosocial risk factors and the occurrence of low back pain.

Abbreviations: GEE, generalised estimating equations; JCQ, Job Content Questionnaire; SMASH, Study on Musculoskeletal disorders, Absenteeism, Stress, and Health.
PARTICIPANTS AND METHODS

Study population
For the SMASH study, workers were recruited from 34 companies located throughout the Netherlands. The participating companies were asked to select workers who had been employed in their current job for at least one year and who were working for 24 hours per week or more. Workers in blue collar jobs, as well as workers in white collar jobs and caring professions were included in the study.

At baseline, 1789 (87%) of the 2064 workers who were invited to participate, completed the questionnaire. Of these, 1738 were eligible for participation in the part of the study focusing on risk factors for low back pain. For the analyses described in this paper, a cohort of 1192 workers with no low back pain at baseline was identified, consisting of workers who reported at baseline that they had not had regular or prolonged low back pain in the previous 12 months.

Baseline survey
Between March 1994 and March 1995 the participants completed a questionnaire and underwent a physical examination. The questionnaire included questions on the individual factors of age, gender, smoking habits, exercise behaviour, and coping skills. Assessment of the body mass index was based on measurements of weight and height taken by a physiotherapist during the physical examination.

Psychosocial work characteristics were assessed by means of a Dutch version of Karasek’s Job Content Questionnaire (JCQ), which includes dimensions on quantitative job demands, decision authority, skill discretion, supervisor support, and coworker support. Conflicting demands were assessed on the basis of one single item from the JCQ.

Flexion and/or rotation of the upper part of the body and moving heavy loads (>25 kg) at work were assessed by means of the Loquest questionnaire. Driving a vehicle at work was also assessed with this questionnaire, and aspects of physical load during leisure time were assessed on the basis of questions comparable to those used to assess the physical load at work.

Assessment of the occurrence of low back pain was based on an adaptation of the Nordic Questionnaire. Workers had to answer the question “Have you had trouble (aches, pain, discomfort) in the low back in the previous 12 months?” with one of the following four response options: no, never; yes, sometimes; yes, regularly; yes, prolonged. A case of low back pain was defined if a worker reported regular or prolonged low back pain in the previous 12 months.

Follow up
After the baseline survey there was a follow up period of three years, and each year the workers received a self administered questionnaire by post. In these questionnaires, the same questions as in the baseline questionnaire were asked to assess exercise behaviour, psychosocial work characteristics, physical load at work and during leisure time, and the occurrence of low back pain in the previous 12 months.

Statistical analysis
Two analytical methods were used: standard regression and GEE. Both methods were carried out with Proc Genmod in the statistical package SAS (version 6.12), and as the outcome variable low back pain is dichotomous, the link function in Proc Genmod was always specified as logistic. Figure 1 illustrates the models that were analysed with the two methods. The regression equations for these models are given in the appendix.

In the standard regression model, the baseline measurements of work related physical risk factors (flexion and/or rotation of the upper part of the body and moving heavy loads) were examined for their association with the occurrence of low back pain. The results of a traditional approach using standard regression analysis and generalised estimating equations differ in both magnitude and precision of the calculated associations.

In the design and analysis of prospective cohort studies on work related risk factors for musculoskeletal symptoms, incorporation of repeated measurements of exposure should be considered. Longitudinal studies involving repeated measurements with relatively short time intervals should be performed to obtain more insight into (the time lag of) the effect of psychosocial work characteristics.

Policy implications
• Reduction of trunk flexion and trunk rotation at work can contribute to the prevention of low back pain.
• Reduction of moving heavy loads at work can contribute to the prevention of low back pain.
• The role of improvement of the psychosocial work environment by reducing quantitative demands and conflicting demands, and increasing supervisor and coworker support in the prevention of low back pain is less clear.

Main messages
• The results of a traditional approach using standard regression analysis and generalised estimating equations differ in both magnitude and precision of the calculated associations.
• In the design and analysis of prospective cohort studies on work related risk factors for musculoskeletal symptoms, incorporation of repeated measurements of exposure should be considered.
loads) and work related psychosocial risk factors (quantitative job demands, conflicting demands, supervisor support, and coworker support) were related to the cumulative incidence of low back pain reported during the three year follow up period. In this analysis, a case of low back pain was defined if a worker reported in at least one of the annual self administered follow up questionnaires, regular or prolonged low back pain in the previous 12 months.

Using GEE, two different models were analysed. In GEE model 1, all risk factors and covariates were assumed to be time independent, which means that only data from the baseline measurement were used, as in the standard regression analysis. These baseline measurements were related to low back pain reported at the three different follow up points. In GEE model 2, all risk factors were time dependent. Most covariates were also time dependent, except for age and gender and the covariates that were only measured at baseline (smoking habits, coping skills, and body mass index). GEE model 2 was also a time lag model, implying that the repeated measurements of the risk factors studied were related to low back pain reported at one measurement point later. Given the fact that in the present study, data on the occurrence of low back pain collected at each measurement point concerned the previous 12 months, the use of a time lag model was necessary to take into account the temporal sequence of cause and effect. GEE model 2 was considered a priori to be the most appropriate model for both the physical and the psychosocial risk factors studied, because it takes into account the time varying nature of both the outcome and the exposure. GEE model 1 was also analysed to be able to obtain insight into the specific effect of taking into account the time varying nature of the exposure by comparison of GEE models 1 and 2.

The analyses of both GEE models were performed using an exchangeable working correlation structure, implying that all correlations between repeated observations of the outcome variable from each subject were assumed to be equal, irrespective of the time period between the measurements. This structure was chosen, because it is the most neutral option, and also because the relatively short follow up period of this study and the identical duration of the intervals between the repeated measurements does not warrant the use of a more specific correlation structure.

In univariate analyses, performed with both analytical methods, crude odds ratios with corresponding 95% confidence intervals were calculated for the risk factors studied. Adjusted odds ratios were determined in a full model, including the work related physical and psychosocial risk factors and the individual factors, other psychosocial work characteristics, other work related physical factors, and physical factors during leisure time that were considered as covariates. Both univariate and multivariable GEE models always included a linear time effect (from 0 to 2).

RESULTS

Table 1 shows the data on reported low back pain for each follow up measurement separately and combined. From the cohort of 1192 workers with no low back pain in the previous 12 months at baseline, data on the occurrence of low back pain were available for 861 workers (72%) for all three annual follow up measurements. These data were used for the analyses with the standard regression method. The cumulative incidence of low back pain in this group during the three year follow up period was 26.6%.

From the cohort of 1192 workers, data on the occurrence of low back pain were available for 1116 workers (94%) for at least one of the follow up measurements. These data were used for the analyses with the GEE method. At each follow up measurement, approximately 13% of workers reported that they had regular or prolonged low back pain in the previous 12 months.

Table 2 gives a detailed overview of the number of reports of low back pain among workers, with data on the occurrence of

<table>
<thead>
<tr>
<th>Number of follow up measurements attended</th>
<th>Number of reports of low back pain (%)</th>
<th>Total number of persons</th>
</tr>
</thead>
<tbody>
<tr>
<td>3</td>
<td>632 (73.4)</td>
<td>138 (16.0)</td>
</tr>
<tr>
<td>2</td>
<td>132 (76.3)</td>
<td>32 (18.5)</td>
</tr>
<tr>
<td>1</td>
<td>71 (86.6)</td>
<td>11 (13.4)</td>
</tr>
</tbody>
</table>

Table 3

<table>
<thead>
<tr>
<th>Risk factor</th>
<th>Change in exposure between baseline and follow up 1 (%)</th>
<th>Change in exposure between follow up 1 and follow up 2 (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>0 levels 1 level 2 levels 0 levels 1 level 2 levels 0 levels 1 level 2 levels</td>
<td></td>
</tr>
<tr>
<td>Flexion and/or rotation of the upper part of the body</td>
<td>658 (61.9) 350 (32.9) 55 (5.2)</td>
<td>675 (71.8) 243 (25.7) 23 (2.4)</td>
</tr>
<tr>
<td>Moving heavy loads (&gt;25 kg)</td>
<td>876 (82.3) 171 (16.1) 18 (1.7)</td>
<td>812 (85.3) 118 (12.4) 12 (2.3)</td>
</tr>
<tr>
<td>Quantitative job demands</td>
<td>682 (64.2) 372 (35.0) 8 (0.8)</td>
<td>628 (66.2) 312 (32.9) 9 (0.9)</td>
</tr>
<tr>
<td>Conflicting demands</td>
<td>672 (63.8) 313 (29.7) 68 (6.5)</td>
<td>646 (68.1) 267 (28.2) 35 (3.7)</td>
</tr>
<tr>
<td>Supervisor support</td>
<td>647 (61.4) 376 (35.7) 31 (2.9)</td>
<td>613 (65.2) 298 (31.7) 29 (3.1)</td>
</tr>
<tr>
<td>Coworker support</td>
<td>746 (70.6) 295 (27.9) 16 (1.5)</td>
<td>662 (69.5) 271 (28.5) 19 (2.0)</td>
</tr>
</tbody>
</table>

*This analysis is based on those workers that provided data on exposure to the specific risk factor, at both baseline and at follow up 1.
†This analysis is based on those workers that provided data on exposure to the specific risk factor at both follow up 1 and follow up 2.
Table 4 Results concerning the relation between work related physical factors and the occurrence of low back pain from multivariable analyses with a traditional approach using standard regression and generalised estimating equations (GEE)*

<table>
<thead>
<tr>
<th>Risk factor</th>
<th>Standard regression model (n=786)</th>
<th>GEE model 1 (n=976)</th>
<th>GEE model 2 (n=976)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Flexion and/or rotation of the upper part of the body</td>
<td>Crude OR (95% CI)†</td>
<td>Adjusted OR (95% CI)‡</td>
<td></td>
</tr>
<tr>
<td>Seldom or never/sometimes</td>
<td>1.00 (1.00 to 1.00)</td>
<td>1.00 (1.00 to 1.00)</td>
<td></td>
</tr>
<tr>
<td>Quite often</td>
<td>1.24 (0.80 to 1.93)</td>
<td>1.10 (0.75 to 1.61)</td>
<td></td>
</tr>
<tr>
<td>Medium level</td>
<td>1.15 (0.71 to 1.84)</td>
<td>0.84 (0.58 to 1.24)</td>
<td></td>
</tr>
<tr>
<td>High level</td>
<td>1.44 (1.07 to 2.55)</td>
<td>1.65 (1.07 to 2.77)</td>
<td></td>
</tr>
</tbody>
</table>

*Crude OR, odds ratio in the population with no missing values for gender, age, smoking habits, body mass index, exercise, physical complaints, psychosocial factors, social support, coworker support, supervisor support, moving heavy loads during leisure time, conflict with colleagues, conflict with supervisor, conflict with organisation, and current level of employment.

†Adjusted OR, odds ratio adjusted for the risk factors mentioned above.

For the work related physical factors studied, higher odds ratios were found for flexion and/or rotation of the upper part of the body and moving heavy loads in GEE model 2. For the highest level of moving heavy loads, the odds ratio in GEE model 2 was slightly lower. The odds ratios for moving heavy loads in GEE model 1 were comparable to those in GEE model 2. A comparison between the adjusted odds ratios resulting from the different analyses shows a similar pattern for both flexion and/or rotation of the upper part of the body and moving heavy loads. In general, the 95% confidence intervals were found to be relatively smaller in the GEE analyses than in the standard regression analyses. With the latter approach, a statistically significant relationship with low back pain was found for flexion and/or rotation of the upper part of the body, but not for moving heavy loads, while with GEE a (borderline) significant relationship with low back pain was found for both flexion and/or rotation of the upper part of the body and moving heavy loads.

Table 5 shows the results for the work related psychosocial risk factors studied. After adjustment for potential confounders, no statistically significant relationship with reported low back pain was found for all significant relationships for both flexion and/or rotation of the upper part of the body and moving heavy loads. In general, the 95% confidence intervals were relative smaller in the GEE analyses than in the standard regression analyses. With the latter approach, a statistically significant relationship with low back pain was found for flexion and/or rotation of the upper part of the body, but not for moving heavy loads, while with GEE a (borderline) significant relationship with low back pain was found for both flexion and/or rotation of the upper part of the body and moving heavy loads.

DISCUSSION
Summary and interpretation of findings
In this article, two different analytical approaches were applied to longitudinal data from a prospective cohort study on work related risk factors for musculoskeletal symptoms. For the work related physical factors studied, higher odds

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Table 5  Results concerning the relation between psychosocial work characteristics and the occurrence of low back pain from multivariable analyses with a traditional approach using standard regression and generalised estimating equations (GEE)*

<table>
<thead>
<tr>
<th>Risk factor</th>
<th>Crude OR (95% CI)†</th>
<th>Adjusted OR (95% CI)‡</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Standard regression model (n=786)</td>
<td>GEE model 1 (n=976)</td>
</tr>
<tr>
<td>Quantitative job demands</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Low (score 6–11)</td>
<td>1.00 (1.00 to 1.00)</td>
<td>1.00 (0.86 to 1.45)</td>
</tr>
<tr>
<td>Medium (score 12–16)</td>
<td>1.43 (0.99 to 2.07)</td>
<td>0.95 (0.68 to 1.31)</td>
</tr>
<tr>
<td>High (score 17–20)</td>
<td>1.87 (0.93 to 3.76)</td>
<td>1.61 (0.89 to 2.93)</td>
</tr>
<tr>
<td>Conflicting demands</td>
<td></td>
<td></td>
</tr>
<tr>
<td>[Strongly] disagree</td>
<td>1.08 (0.75 to 1.57)</td>
<td>1.21 (0.88 to 1.66)</td>
</tr>
<tr>
<td>Agree</td>
<td>1.53 (0.84 to 2.79)</td>
<td>1.23 (0.72 to 2.08)</td>
</tr>
<tr>
<td>Supervisor support</td>
<td></td>
<td></td>
</tr>
<tr>
<td>High (score 13–16)</td>
<td>1.42 (0.84 to 2.40)</td>
<td>1.16 (0.73 to 1.84)</td>
</tr>
<tr>
<td>Medium (score 11–12)</td>
<td>1.69 (0.97 to 2.94)</td>
<td>1.40 (0.87 to 2.26)</td>
</tr>
<tr>
<td>Low (score 4–10)</td>
<td>1.00 (1.00 to 1.00)</td>
<td>1.00 (1.00 to 1.00)</td>
</tr>
<tr>
<td>Coworker support</td>
<td></td>
<td></td>
</tr>
<tr>
<td>High (score 13–16)</td>
<td>1.36 (0.91 to 2.05)</td>
<td>1.33 (0.92 to 1.93)</td>
</tr>
<tr>
<td>Medium (score 11–12)</td>
<td>1.68 (0.91 to 3.10)</td>
<td>1.42 (0.82 to 2.44)</td>
</tr>
</tbody>
</table>

*The different models that were analysed are illustrated in fig 1.
†Crude OR, odds ratio in the population with no missing values for gender, age, smoking habits, body mass index, exercise behaviour during leisure time, coping skills (active problem solving, avoidance behaviour, social support seeking), moving heavy loads during leisure time, flexion and/or rotation of the upper part of the body during leisure time, driving a vehicle during leisure time, moving heavy loads at work, flexion and/or rotation of the upper part of the body at work, driving a vehicle at work, and the other psychosocial work characteristics mentioned in the table. ‡Adjusted OR, odds ratio adjusted for the risk factors mentioned above.

In addition to differences in the magnitude of the odds ratios, differences in the precision of the estimates could be observed. The confidence intervals for the adjusted odds ratios were smaller than those of the odds ratios resulting from the traditional standard regression model. This can be explained by the fact that all available outcome data can be included in the GEE model, in the present study a total of 76% of workers reported the same level of exposure, both at baseline and at the first two follow up measurements (data not shown). For moving heavy loads, taking into account the time varying nature of the exposure did not change the findings. The overview of changes in reported exposure between the baseline and at the first two follow up measurements also showed that changes in exposure have apparently occurred in the case of moving heavy loads, while the exposure to flexion and/or rotation of the upper part of the body, both at baseline and at the first two follow up measurements, remained relatively stable. For both high quantitative job demands and high conflict demands, the comparison of GEE model 2 with GEE model 1 showed that taking into account the time varying nature of the exposure led to a decrease in the odds ratio for low coworker support, whereas the opposite was found for low supervisor support. This cannot be explained by the fact that all available outcome data can be included in the GEE model. In the present study a total of 76% of workers reported the same level of exposure, both at baseline and at the first two follow up measurements. Additionally, in the GEE model 2 the model that was considered to be the most appropriate, weaker results for the psychosocial work characteristics were found than in the analysis of the traditional standard regression model. For both high quantitative job demands and high conflict demands, the comparison of GEE model 2 with GEE model 1 showed that taking into account the time varying nature of the exposure led to a decrease in the odds ratio for low coworker support, whereas the opposite was found for low supervisor support.
of the follow up measurements were included in the GEE analyses. For the majority of these workers, more than one observation was also included in the analyses, which resulted in even more power. Only for moving heavy loads did the increase in power result in a different conclusion with regard to the presence of a statistically significant relationship with low back pain.

**Limitations and potential sources of bias**

Only the two GEE models included in the present analysis were taken into consideration, although other possibilities do exist. The time lag model, the preferred model for the present data, takes into account the temporal sequence of cause and effect, and this model can also be extended to models with different time lags. By repeatedly measuring exposure and outcome, the biologically relevant exposure window at some fixed interval of time relative to the outcome event can be defined. The length of the exposure window and its temporal position relative to the outcome event will depend on the supposed causal mechanism for the exposure of interest. When the understanding of disease aetiology is too limited to specify a credible temporal relationship, different time lags can be studied to obtain more insight into the hypothesised relationships. It is beyond the scope of this paper to examine all these possibilities, but it is clear that modelling approaches such as the GEE method, make it feasible to explore these issues in the context of epidemiological cohort studies with repeated measurements of exposure and health data.

One can imagine that, especially with regard to the psychosocial work characteristics, the postulation of different time lags could provide insight into the nature of the relationship of these variables with low back pain. The inclusion of an appropriate time lag is especially important for exposures that are relatively unstable. The psychosocial work environment is clearly subject to change. It can be hypothesised that changes in the psychosocial work environment occur more frequently than changes in the physical work environment, and that psychosocial work characteristics may have a more short term effect on low back pain. Consequently, shorter intervals between the repeated measurements would be necessary to make an adequate assessment of the role of psychosocial work characteristics. Another explanation for the difference in results for physical and psychosocial exposures might be that the physical exposures have a much more immediate effect, whereas the psychosocial exposures need to accumulate over time before they start to have an effect on low back pain.

In the GEE analyses, a maximum of 116 workers with data on the occurrence of low back pain for at least one of the follow up measurements could be included. This was done under the assumption that the pattern of missing data on the occurrence of low back pain during the follow up is random. It is not possible to verify completely whether this assumption holds. However, the incidence of low back pain at the first follow up did not differ for those workers who were lost to follow up after this specific measurement (data not shown).

A specific limitation of the analyses of work related physical risk factors described in the present paper is that all measurements were based on self reports. In the SMASH study, physical load at work was also quantified by means of analyses of video recordings. However, as these measurements were not repeated at the annual follow up measurements, these data are not included in this paper. In general, the results of the present analyses, based on self reported measures of physical load at work, are in accordance with the results of the previously reported analyses of quantified measures based on the observations of baseline video recordings.

**Conclusion**

In conclusion, the results of this study clearly show that there are differences between the two analytical approaches applied, in both magnitude and precision of the calculated odds ratios. Compared with the traditional approach using standard regression analysis, GEE analysis with a time lag model, in which the time varying nature of both the exposure and the outcome is taken into account, revealed stronger associations for the work related physical risk factors studied and weaker associations for the psychosocial work characteristics. Moreover, for moving heavy loads, conclusions on the presence or absence of a statistically significant relationship with low back pain differed, depending on the analytical approach used. The analyses of another model with the GEE method provided insight into the specific effect of taking into account the time varying nature of the exposure. This appeared to have an influence on the results.

This paper clearly shows that in the design and analysis of prospective cohort studies on work related risk factors for
musculoskeletal symptoms, the incorporation of repeated measurements of exposure should be considered. GEE analysis provides a means of dealing with this kind of data. An additional advantage is that changes in outcome, that apparently occur in case of an episodic outcome event, can also be taken into account. To encourage researchers to carry out such studies, discussions should be initiated to determine the appropriate intervals between the repeated measurements and also the appropriate number of repeated measurements needed to study both work related physical and, in particular, psychosocial risk factors for low back pain.

ACKNOWLEDGEMENTS
The Study on Musculoskeletal disorders, Absenteeism, Stress, and Health (SMASH) was financially supported by the Dutch Ministry of Social Affairs and Employment, the Dutch Ministry of Public Health, Welfare and Sports, and the Dutch National Institute for Social Security.

APPENDIX: REGRESSION EQUATIONS FOR THE MODELS ILLUSTRATED IN FIG 1

Standard regression model:

\[
\ln\left(\frac{P(Y_{it} = 1)}{P(Y_{it} = 0)}\right) = \beta_0 + \beta_1 x_{i,t-1} + \ldots + \beta_p x_{i,t-1}
\]

where: \( Y_{it} = \) binary outcome for subject \( i \) at time \( t \), \( \beta_0 = \) intercept, \( x_{i,t} = \) independent variable \( x_i \) of subject \( i \) at time \( t-1 \), \( \exp(\beta_p) = \) odds ratio of independent variable \( x_p \).

GEE model 1:

\[
\ln\left(\frac{P(Y_{it} = 1)}{P(Y_{it} = 0)}\right) = \beta_0 + \beta_1 x_{i,t0} + \ldots + \beta_p x_{i,t0}
\]

where: \( Y_{it} = \) binary outcome for subject \( i \) at time \( t \), \( \beta_0 = \) intercept, \( x_{i,t0} = \) independent variable \( x_i \) of subject \( i \) at time \( t=0 \), \( \exp(\beta_p) = \) odds ratio of independent variable \( x_p \).

GEE model 2:

\[
\ln\left(\frac{P(Y_{it} = 1)}{P(Y_{it} = 0)}\right) = \beta_0 + \beta_1 x_{i,t-1} + \ldots + \beta_p x_{i,t-1}
\]

where: \( Y_{it} = \) binary outcome for subject \( i \) at time \( t \), \( \beta_0 = \) intercept, \( x_{i,t-1} = \) independent variable \( x_i \) of subject \( i \) at time \( t-1 \), \( \exp(\beta_p) = \) odds ratio of independent variable \( x_p \).

REFERENCES